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1. Let $UIA + IAU + AUI = 999$, where each letter correspond to some digit differ than 0. If $U > I > A$ then largest possible value of U equal to

- (A) 3 (B) 4 (C) 5 (D) 6 (E) 7

2. Let arithmetic mean of two numbers a and b equal to 5 and arithmetic mean of three numbers a , b and c equal to 6. Then c equal to

- (A) 5 (B) 6 (C) 7 (D) 8 (E) 11

3. Let geometric mean of two numbers a and b equal to 5 and geometric mean of three numbers a , b and c equal to 6. Then c equal to

- (A) 1.2 (B) 1.44 (C) 4.68 (D) 6.48 (E) 8.64

4. Consider equation $ax + b = cx + d$. This equation has single solution if

- (A) $a=c$ (B) $a=d$ (C) $b=c$ (D) $b \neq d$ (E) $a \neq c$

5. Consider equation $ax + b = cx + d$. This equation has infinitely many solutions if

- (A) $a=c$ and $b=d$ (B) $a=c$ and $b \neq d$ (C) $a \neq c$ and $b=d$ (D) $a \neq c$ and $b \neq d$ (E) $ab=cd$

6. Consider equation $ax + b = cx + d$. This equation has no solution if

- (A) $a=c$ and $b=d$ (B) $a=c$ and $b \neq d$ (C) $a \neq c$ and $b=d$ (D) $a \neq c$ and $b \neq d$ (E) $ab=cd$

7. If for positive a, b and c $\frac{1}{a+b} < \frac{1}{b+c}$ then we have following

- (A) $a < c$ (B) $a > c$ (C) $a > b$ (D) $a < b$ (E) $b < a+c$

8. How many positive integer x satisfy following inequality: $\frac{1}{x+3} > 0.07$?

- (A) 7 (B) 9 (C) 11 (D) 13 (E) 14

9. How many positive integers x satisfy following double inequalities: $0.13 > \frac{1}{x+3} > 0.07$?

- (A) 7 (B) 9 (C) 11 (D) 13 (E) 14

10. Let two positive real numbers a and b satisfy equality $\frac{a+b}{2} = \sqrt{ab}$, i.e. their arithmetic mean equal to its geometric mean. Then

- (A) $a > b$ (B) $a < b$ (C) $a = b$ (D) $a = 2b$ (E) $b = 2a$

11. Let three positive real numbers a, b and c satisfy equality $\frac{a+b+c}{3} = \sqrt[3]{abc}$, i.e. their arithmetic mean equal to its geometric mean. Then

- (A) $a > b = c$ (B) $a < b < c$ (C) $a = b = c$ (D) $a = b > c$ (E) $a = b < c$

12. Let x_1 and x_2 be the roots of the following quadratic equation $0.156x^2 - 0.013x - 0.013 = 0$. Find $x_1 + x_2$.

- (A) -0.013 (B) 0.013 (C) 0.156 (D) 1/12 (E) -1/12

13. Let x_1 and x_2 be the roots of the following quadratic equation $0.156x^2 - 0.013x - 0.013 = 0$. Find $x_1 \cdot x_2$.

- (A) -0.013 (B) 0.013 (C) 0.156 (D) 1/12 (E) -1/12

14. Let x_1 and x_2 be the roots of the following quadratic equation $0.156x^2 - 0.013x - 0.013 = 0$. Find $\frac{1}{x_1} + \frac{1}{x_2}$.

- (A) 12 (B) -12 (C) 2 (D) -1 (E) 1

15. Let x_1 and x_2 be the roots of the following quadratic equation $0.156x^2 - 0.013x - 0.013 = 0$. Find $x_1^2 + x_2^2$.

- (A) 29/144 (B) -29/144 (C) 25/144 (D) -23/144 (E) 23/144

16. Let x_1 and x_2 be the roots of the following quadratic equation $0.156x^2 - 0.013x - 0.013 = 0$. Find $x_1^3 + x_2^3$.

- (A) 31/1728 (B) -35/1728 (C) 35/1728 (D) 37/1728 (E) -37/1728

17. If for $a_1 = -1$, $a_2 = 2$ and for $n \geq 3$ $a_n = \frac{a_{n-1}}{a_{n-2}}$, then a_{2009} equal to

- (A) 2 (B) 1/2 (C) -1/2 (D) -1 (E) -2

18. How many integer solutions does the following system of inequalities have? $\begin{cases} x^2 - y < -1 \\ x^2 + y < 5 \end{cases}$?

- (A) more than 5 (B) 5 (C) 4 (D) 3 (E) 2

19. For given triangle ΔABC let

$$3 \angle A - \angle B = 98^\circ 35''$$

$$4 \angle B - \angle C = 168^\circ$$

$$3 \angle C - \angle A = 143^\circ.$$

Find $\angle B$.

- (A) $94^\circ 35''$ (B) $94^\circ 25''$ (C) $49^\circ 35''$ (D) $49^\circ 25''$ (E) $98^\circ 35''$

20. For given triangle ΔABC let $\angle A = \angle C$ and $AB=5$ sm. Find $2BC+3AB$.

- (A) 10 (B) 15 (C) 20 (D) 25 (E) 30

21. For given triangle ΔABC let $AB=BC$ and $\angle C = 80^\circ$. Find $3 \angle B + 2 \angle A$.

- (A) 80° (B) 160° (C) 180° (D) 200° (E) 220°

22. For given triangle ΔABC let $AB=BC=5$, $BD \perp AC$ and $BD=3$. Find area of the triangle.

- (A) 10 (B) 12 (C) 14 (D) 16 (E) 18

23. For given triangle ΔABC let $AB=BC=5$, $BD \perp AC$ and $BD=3$. Find perimeter of the triangle.

- (A) 18 (B) 19 (C) 20 (D) 21 (E) 22

24. Let D be point on BC such that $AB+BD=AC$ and $\angle BAD = \angle DAC = 30^\circ$. Then $\angle ACB$ equal to

- (A) 50 (B) 48 (C) 45 (D) 40 (E) 30

25. In ΔABC , the height $AD=h_1$ and the height $CE=h_2$ and $\angle ABC = 30^\circ$. Find the area of ΔABC .

- (A) $2h_1h_2$ (B) h_1h_2 (C) $\frac{1}{2}h_1h_2$ (D) $(h_1 + h_2)^2$ (E) $h_1^2 + h_2^2$

26. If for given positive integers a and b their sum $a+b$ and product ab are even then we have following

- (A) a -odd, b -even (B) a -odd, b -odd (C) a -even, b -odd (D) a -even, b -even (E) There are not such numbers

27. If for given positive integers a and b their sum $a+b$ and product ab are odd then we have following

- (A) a -odd, b -even (B) a -odd, b -odd (C) a -even, b -odd (D) a -even, b -even (E) There are not such numbers

28 . If a is divisible by 3 and b is divisible by 9 then their sum $(a+b)$ is divisible by

- (A) 3 (B) 6 (C) 9 (D) 12 (E) 18

29 . If a is divisible by 3 and b is divisible by 9 then their product (ab) is divisible by

- (A) 3 (B) 9 (C) 27 (D) 12 (E) 18

30. The floor of a rectangular room is covered with square tiles. The width of the room counts m tiles, the length counts n tiles ($n \geq m$). Half the number of tiles lie at the edges of the room. For how many values of the dimensions (width and length) of the room is this possible?

- (A) none (B) 1 (C) 2 (D) 3 (E) more than 3

31 . If the remainder when a is divided by 5 is 2, and the remainder when b is divided by 5 is 4, find the remainder when (ab) is divided by 5.

- (A) 0 (B) 1 (C) 2 (D) 3 (E) 4

32 . If the remainder when a is divided by 5 is 2, find the remainder when $(4a-3)$ is divided by 5.

- (A) 0 (B) 1 (C) 2 (D) 3 (E) 4

33 . If the remainder when a is divided by 5 is 2, find the remainder when (a^2+3a+4) is divided by 5.

- (A) 0 (B) 1 (C) 2 (D) 3 (E) 4

34 . How many divisors have 36 including 1 and itself?

- (A) 3 (B) 6 (C) 9 (D) 12 (E) 18

35 . How many divisors have 2^{2009} including 1 and given number itself?

- (A) 2008 (B) 2009 (C) 2010 (D) 2011 (E) 2012

36 . How many divisors have $2^6 \cdot 3^{19}$ including 1 and given number itself?

- (A) 25 (B) 114 (C) 120 (D) 133 (E) 140